## The McGraw-Hill Companies

## Chapter 29

## Cryptography

 andNetwork Security


## OBJ ECTI VES:

$\square$ To introduce security goals and to discuss the types of attacks that threaten these goals.
$\square$ To introduce traditional ciphers as symmetric-key ciphers to create the background for understanding modern symmetric-key ciphers.
$\square$ To introduce the elements of modern block ciphers and show an example of a modern block cipher in which these elements are used.

To discuss the general idea behind asymmetric-key ciphers and introduce one common cipher in this category.
$\square$ To discuss message integrity and show how to use a cryptographic hash function to create a message digest.

## OBJ ECTI VES (continued):

$\square$ To introduce the idea of message authentication and show how a message digest combined with a secret can authenticate the sender.
$\square$ To show how the idea of digital signatures can be used to authenticate a message using a pair of private-public keys.
$\square$ To introduce the idea of entity authentication and show some simple schemes using either a secret key or a pair of privatepublic keys.
$\square$ To show how secret keys in symmetric-key cryptography and how public keys in asymmetric-key cryptography can be distributed and managed using KDCs or certificate authorities (CAs).

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Outline 29.2 Traditional Ciphers
29.3 Modern Ciphers
29.4 Asymmetric-Key Ciphers
29.5 Message Integrity
29.6 Message Authentication
29.7 Digital Signature
29.8 Entity Authentication
29.9 Key Management

## 29-1 INTRODUCTION

We are living in the information age. We need to keep information about every aspect of our lives. In other words, information is an asset that has a value like any other asset. As an asset, information needs to be secured from attacks. To be secured, information needs to be hidden from unauthorized access (confidentiality), protected from unauthorized change (integrity), and available to an authorized entity when it is needed (availability).

## Topics Discussed in the Section

$\checkmark$ Security Goals
$\checkmark$ Attacks
$\checkmark$ Services
$\checkmark$ Techniques

Figure 29.1 Taxonomy of attacks with relation to security goals


## 29-2 TRADITIONAL CIPHERS

We now look at the first goal of security, confidentiality. Confidentiality can be achieved using ciphers. Traditional ciphers are called symmetric-key ciphers (or secret-key ciphers) because the same key is used for encryption and decryption and the key can be used for bidirectional communication. Figure 29.2 shows the general idea behind a symmetric-key cipher.

## Topics Discussed in the Section

$\checkmark$ Key
$\checkmark$ Substitution Ciphers
$\checkmark$ Transposition Ciphers
$\checkmark$ Stream and Block Ciphers

Figure 29.2 General idea of traditional cipher


## Note

## A substitution cipher replaces one symbol with another.

Figure 29.3 Symmetric-key: locking and unlocking with the same key


## Note

## A substitution cipher replaces one symbol with another.

Figure 29.4 Representation of characters in modulo 26


## Note

# In additive cipher, the plaintext, ciphertext, and key are integers in modulo 26. 

## Example 29.1

Use the additive cipher with key = 15 to encrypt the message "hello".

## Solution

We apply the encryption algorithm to the plaintext, character by character. The result is "WTAAD". Note that the cipher is monoalphabetic because two instances of the same plaintext character (Is) are encrypted as the same character (A).

```
Plaintext: h }->0
Plaintext: e }->0
Plaintext: l }->1
Plaintext: 1 }->1
Plaintext: o }->1
```

Ciphertext: $22 \rightarrow$ W
Ciphertext: $19 \rightarrow$ T
Ciphertext: $00 \rightarrow$ A
Ciphertext: $00 \rightarrow$ A
Ciphertext: $03 \rightarrow$ D

```
Encryption: (07 + 15) mod 26
```

Encryption: (07 + 15) mod 26
Encryption: (04+15) mod 26
Encryption: (04+15) mod 26
Encryption: (11+15) mod 26
Encryption: (11+15) mod 26
Encryption: (11+15) mod 26
Encryption: (11+15) mod 26
Encryption: (14+15) mod 26

```
Encryption: (14+15) mod 26
```


## Example 29.2

Use the additive cipher with key $=15$ to decrypt the message "WTAAD".

## Solution

We apply the decryption algorithm to the plaintext character by character. The result is "hello". Note that the operation is in modulo 26, which means that we need to add 26 to a negative result (for example -15 becomes 11).

Figure 29.5 An example key for mono-alphabetic substitution cipher

| Plaintext $\longrightarrow$ a |  | c |  |  | e | f | g | h | i | j | k | 1 | m | n | , | o | p | q |  | s | t | U | - | v | w | x | y | z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ciphertext $\rightarrow$ N | NO | A | A | T | R | B | E | C | F | U | X | D | Q | Q | G | Y | L | K |  | H V | I | J | J M | M | P | Z | S | W |

## Example 29.3

## We can use the key in Figure 29.5 to encrypt the message

this message is easy to encrypt but hard to find the key

The ciphertext is

ICFVQRVVNEFVRNVSIYRGAHSLIOJICNHTIYBFGTICRXRS

## A transposition cipher reorders symbols.



## 29-3 MODERN CIPHERS

The traditional symmetric-key ciphers that we have studied so far are character-oriented ciphers. With the advent of the computer, we need bit-oriented ciphers. This is because the information to be encrypted is not just text; it can also consist of numbers, graphics, audio, and video data. It is convenient to convert these types of data into a stream of bits, to encrypt the stream, and then to send the encrypted stream. A modern block cipher can be either a block cipher or a stream cipher.

## Topics Discussed in the Section

$\checkmark$ Modern Block Ciphers
$\checkmark$ Data Encryption Standard (DES)
$\checkmark$ Modern Stream Ciphers






## Example 29.4

We choose a random plaintext block, a random key, and a computer program to determine what the ciphertext block would be (all in hexadecimal):

Key:
AABB09182736CCDD

CipherText:
C0B7A8D05F3A829C

## Example 29.5

To check the effectiveness of DES, when a single bit is changed in the input, let us use two different plaintexts with only one single bit difference. The two ciphertexts are completely different without even changing the key:

```
    Plaintext:
0000000000000000
    Plaintext:
0000000000000001
```

```
    Key:
22234512987ABB23
    Key:
22234512987ABB23
```

    Ciphertext:
    4789FD476E82A5F1
    Ciphertext:
    0A4ED5C15A63FEA3

Although the two plaintext blocks differ only in the rightmost bit, the ciphertext blocks differ in 29 bits.


## 29-4 ASYMMETRIC-KEY CIPHERS

In previous sections we discussed symmetric-key ciphers. In this chapter, we start the discussion of asymmetric-key ciphers. Symmetric-key and asymmetric-key ciphers will exist in parallel and continue to serve the community. We actually believe that they are complements of each other; the advantages of one can compensate for the disadvantages of the other.

## Topics Discussed in the Section

$\checkmark$ Keys
$\checkmark$ General Idea
$\checkmark$ RSA Cryptosystem
$\checkmark$ Applications

## Note

Symmetric-key cryptography is based on sharing secrecy;
asymmetric-key cryptography is based
on personal secrecy.

## Note

In symmetric-key cryptography, symbols are permuted or substituted; in asymmetric-key cryptography, numbers are manipulated.


Note

## Asymmetric-key ciphers are sometimes called public-key ciphers.

Figure 29.14 General idea of asymmetric-key cryptosystem



## Example 29.6

For the sake of demonstration, let Bob choose 7 and 11 as $p$ and $q$ and calculate $n=7 \times 11=77$. The value of $\varphi(\mathrm{n})=$ (7-1)(11-1), or 60 . If he chooses $e$ to be 13 , then $d$ is 37 . Note that $e \times d \bmod 60=1$. Now imagine that Alice wants to send the plaintext 5 to Bob. She uses the public exponent 13 to encrypt 5 . This system is not safe because $p$ and $q$ are small.

```
Plaintext: 5
C=5 53}=26 mod 77
Ciphertext: }2
```

```
Ciphertext:26
P}=2\mp@subsup{6}{}{37}=5\operatorname{mod}7
Plaintext: 5
```


## Example 29.7

Here is a more realistic example calculated with a computer. We choose a 512-bit $p$ and $q$, calculate $n$ and $\varphi(n)$, We then choose e and calculate d. Finally, we show the results of encryption and decryption. The integer $p$ is a 159 -digit number.

```
p= 961303453135835045741915812806154279093098455949962158225831508796
479404550564706384912571601803475031209866660649242019180878066742
1096063354219926661209
```

The integer $q$ is a 160 -digit number.
$q=$

```
120601919572314469182767942044508960015559250546370339360617983217
    314821484837646592153894532091752252732268301071206956046025138871
    45524969000359660045617
```


## Example 29.7 Continued

## The modulus $n=p \times q$. It has 309 digits.

$$
n=\left\lvert\, \begin{array}{l|l}
n & 115935041739676149688925098646158875237714573754541447754855261376 \\
147885408326350817276878815968325168468849300625485764111250162414 \\
552339182927162507656772727460097082714127730434960500556347274566 \\
628060099924037102991424472292215772798531727033839381334692684137 \\
327622000966676671831831088373420823444370953
\end{array}\right.
$$

$$
\varphi(n)=(p-1)(q-1) \text { has } 309 \text { digits. }
$$

$$
\phi(n)=\left\lvert\, \begin{aligned}
& 115935041739676149688925098646158875237714573754541447754855261376 \\
& 147885408326350817276878815968325168468849300625485764111250162414 \\
& 552339182927162507656751054233608492916752034482627988117554787657 \\
& 013923444405716989581728196098226361075467211864612171359107358640 \\
& \\
& 614008885170265377277264467341066243857664128
\end{aligned}\right.
$$

## Example 29.7 Continued

Bob chooses $e=35535$ (the ideal is 65537). He then finds $d$.

| $\boldsymbol{e}=$ | 35535 |
| :--- | :--- |
| $\boldsymbol{d}=$ | 580083028600377639360936612896779175946690620896509621804228661113 |
|  | 805938528223587317062869100300217108590443384021707298690876006115 |
|  | 306202524959884448047568240966247081485817130463240644077704833134 |
|  | 010850947385295645071936774061197326557424237217617674620776371642 |
|  | 0760033708533328853214470885955136670294831 |

Alice wants to send the message "THIS IS A TEST", which can be changed to a numeric value using the 00-26 encoding scheme (26 is the space character).

$$
\mathbf{P}=\quad 1907081826081826002619041819
$$

## Example 29.7 Continued

The ciphertext calculated by Alice is $\mathrm{C}=\mathrm{P}^{e}$, which is
$\mathbf{C}=\quad 475309123646226827206365550610545180942371796070491716523239243054$ 452960613199328566617843418359114151197411252005682979794571736036 101278218847892741566090480023507190715277185914975188465888632101 148354103361657898467968386763733765777465625079280521148141844048 14184430812773059004692874248559166462108656

Bob can recover the plaintext from the ciphertext using $\mathrm{P}=\mathrm{C}^{d}$, which is

$$
\mathbf{P}=
$$

$$
1907081826081826002619041819
$$

The recovered plaintext is "THIS IS A TEST" after decoding.

## 29-5 MESSAGE INTEGRITY

The cryptography systems that we have studied so far provide secrecy, or confidentiality, but not integrity. However, there are occasions where we may not even need secrecy but instead must have integrity. For example, Alice may write a will to distribute her estate upon her death. The will does not need to be encrypted. After her death, anyone can examine the will. The integrity of the will, however, needs to be preserved. Alice does not want the contents of the will to be changed.

## Topics Discussed in the Section

$\checkmark$ Message and Message Digest
$\checkmark$ Hash Functions


## The message digest needs to be safe from change.

## 29-6 MESSAGE AUTHENTICATION

A digest can be used to check the integrity of a message: that the message has not been changed. To ensure the integrity of the message and the data origin authentication - that Alice is the originator of the message, not somebody else-we need to include a secret held by Alice (that Eve does not possess) in the process; we need to create a message authentication code (MAC). Figure 29.17 shows the idea.

## Topics Discussed in the Section

$\checkmark$ MAC
$\checkmark$ HMAC


## Note

## A MAC provides message integrity and message authentication using a combination of a hash function and a secret key.

## 29-7 DIGITAL SIGNATURE

Another way to provide message integrity and message authentication (and some more security services as we see shortly) is a digital signature. A MAC uses a secret key to protect the digest; a digital signature uses a pair of private-public keys.

## Topics Discussed in the Section

$\checkmark$ Comparison
$\checkmark$ Process
$\checkmark$ Signing the Digest
$\checkmark$ Services
$\checkmark$ RSA Digital Signature Scheme
$\checkmark$ Digital Signature Standard (DSS)

## Note

## A digital signature uses a pair of privatepublic keys.



## Note

A digital signature needs a public-key system.
The signer signs with her private key; the verifier verifies with the signer's public key.

## Note

## A cryptosystem uses the private and public keys of the receiver:

a digital signature uses the private and public keys of the sender.



Figure 29.21 The RSA signature one the message digest


## 29-8 ENTITY AUTHENTICATION

Entity authentication is a technique designed to let one party prove the identity of another party. An entity can be a person, a process, a client, or a server. The entity whose identity needs to be proven is called the claimant; the party that tries to prove the identity of the claimant is called the verifier.

## Topics Discussed in the Section

$\checkmark$ Entity versus Message Authentication
$\checkmark$ Verification Categories
$\checkmark$ Passwords
$\checkmark$ Challenge-Response

## Note

## In challenge-response authentication, the claimant proves that she knows a secret without sending it to the veriffier.

Figure 29.22 Unidirectional symmetric-key authentication



Figure 29.24 Digital signature, unidirectional authentication


## 29-9 KEY MANAGEMENT

We discussed symmetric-key and asymmetric-key cryptography in the previous sections. However, we have not yet discussed how secret keys in symmetric-key cryptography, and public keys in asymmetric-key cryptography, are distributed and maintained. This section touches on these two issues.

## Topics Discussed in the Section

$\checkmark$ Symmetric-Key Distribution
$\checkmark$ Symmetric-Key Agreement
$\checkmark$ Public-Key Distribution


## Note

## A session symmetric key between two parties is used only once.

KA Encrypted with Alice-KDC secret key
Session key between Alice and Bob
$K_{B}$ ही Encrypted with Bob-KDC secret key


Figure 29.27 Diffie-Hellman method


## Note

The symmetric (shared) key in the Diffie-Hellman method is $K=g^{x y} \bmod p$.

## Example 29.8

Let us give a trivial example to make the procedure clear. Our example uses small numbers, but note that in a real situation, the numbers are very large. Assume that $g=7$ and $p=23$. The steps are as follows:

1. Alice chooses $x=3$ and calculates $\mathrm{R}^{1}=7^{3} \bmod 23=21$.
2. Alice sends the number 21 to Bob.
3. Bob chooses $y=6$ and calculates $R_{2}=7^{6} \bmod 23=4$.
4. Bob sends the number 4 to Alice.
5. Alice calculates the symmetric key $\mathrm{K}=4^{3} \bmod 23=18$. Bob calculates the symmetric key K=216 $\bmod 23=18$.

The value of K is the same for both Alice and Bob; $g^{\star y} \bmod p=7^{18} \bmod 35=18$.

## Note

## In public-key cryptography, everyone has access to everyone's public key; public keys are available to the public.



